

EE103 Final Examination

Dec. 12, 2017 4:00-7:00 p.m.

Name _____ ID _____

i. You are allowed to use **2 pages of formulas and tables**, but not any concept descriptions or derivations.

ii. Please fill the score blanks below:

Qz1 _____ Qz2 _____ Qz3 _____ Qz4 _____

Qz5 _____ Qz6 _____ Qz7 _____ Qz8 _____

Delete two lowest scores and provide the average of 6 quizzes in 2 decimal points
Average= _____.

Midterm Exam Score (modified)= _____.

lii. The final course grade will be based on the following weights

Quiz Average 20%

Midterm Exam 30%

Final Exam 50%

Final Exam provides 6 Problems

[1] 20 points _____

[2] 15 points _____

[3] 20 points _____

[4] 20 points _____

[5] 20 points _____

[6] 5 points _____

Total 100 points _____

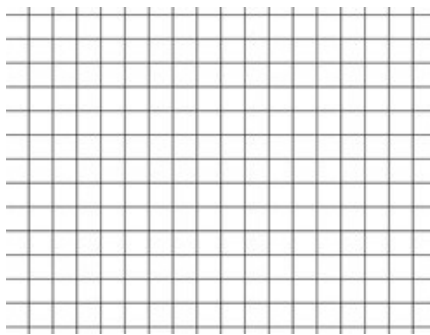
[1] (20points) Given a function $x(t) = 2(t + 1) u(t+1) - 2t u(t) - 2 u(t-2)$

a new function $x_1(t)$ is defined as **$x_1(t) = 2 x_{\text{even}}(t) + x_{\text{odd}}(t)$** .

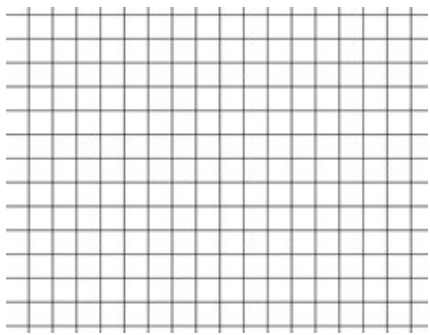
Plot $x_{\text{even}}(t)$, $x_{\text{odd}}(t)$ and $x_1(t)$ on the graph below.



plot $x_{\text{even}}(t)$ here (5 points)



plot $x_{\text{odd}}(t)$ here (5 points)

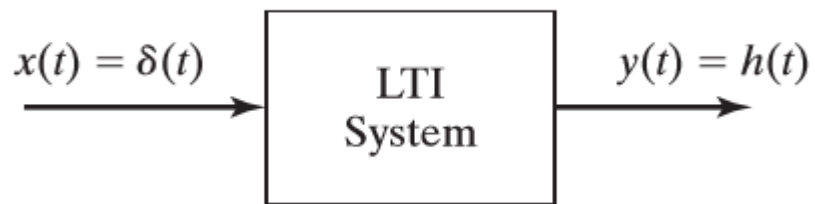


plot $x_1(t)$ here (5 points)

Express $x_1(t)$ mathematically

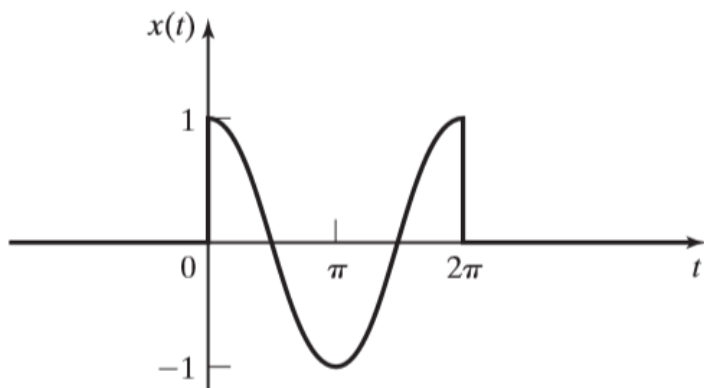
(5points)

[2] (15 points) A linear time-invariant (LTI) system is described represented below.



For $h(t) = e^{-3t} u(t)$ and $x(t) = \text{rect}(t/2)$, find $y(t)$ by using $y(t) = x(t) * h(t) = h(t) * x(t)$.

[3] (30 points) A windowed function is plotted below.



(a) (10 points) **Write down a mathematical description of $x(t)$** by using the cosine and rectangular functions.

$$x(t) = (\quad) \times (\quad)$$

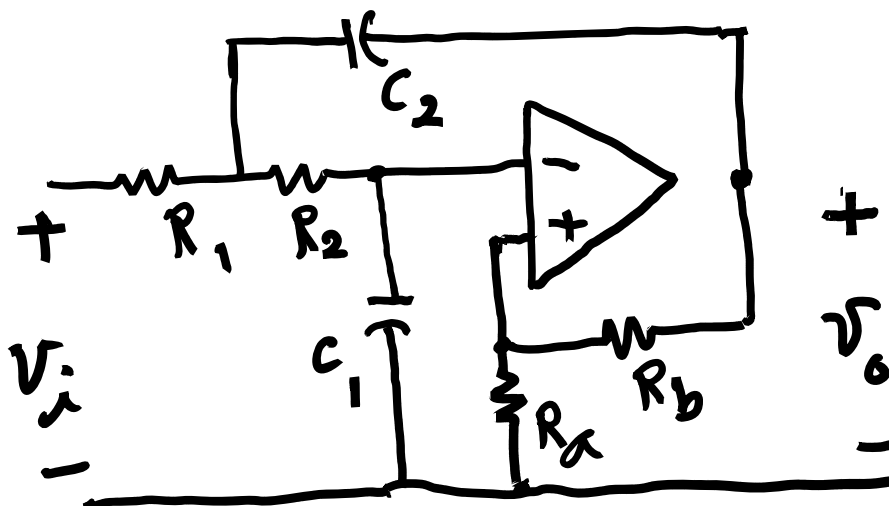
$$\text{Let } x_1(t) = x(t) \times \sum_{k=-\infty}^{\infty} \delta(t - k3\pi)$$

(b) (20 points) **Find Fourier transform of $x_1(t)$.**

Step 1 (10pts) First find $X(\omega)$

Step 2 (10pts) Find $X_1(\omega)$

[4] (20 points) Let us consider the following OP amp circuit.

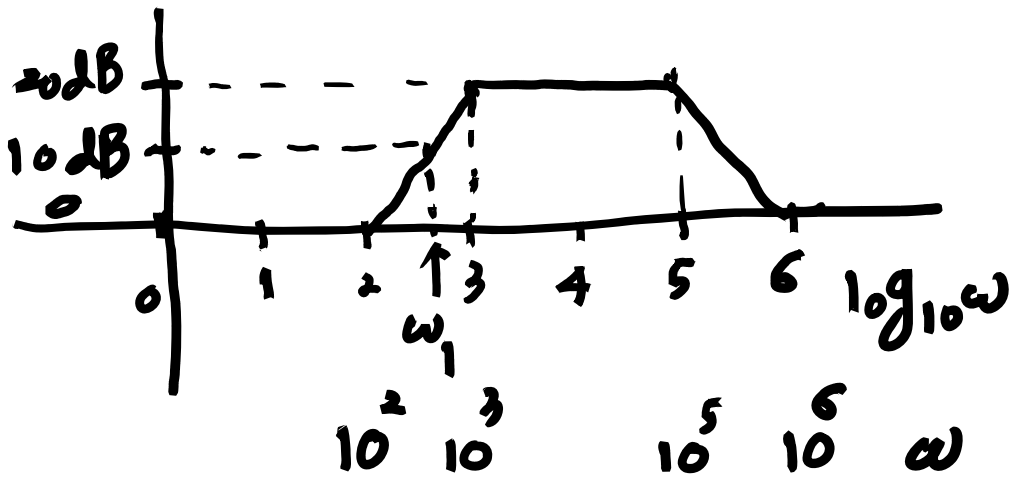


Let $C_1 = 2 C_2 = 1 \mu\text{F}$, all resistance values are $1\text{M}\Omega$

(a) (15points) Find $H(s) = V_o(s)/V_i(s)$

(b) (5 points) **Find $h(t)$** by taking inverse Laplace transform of $H(s)$.

[5].(20 points) The following figure show a Bode plot of a band-pass filter.



At $\omega = \omega_1$, the gain in dB is 10 dB.

(a). (10 points) Find the corresponding $H(j\omega)$ with identification of all zero and pole (angular) frequencies. Hint: $H(j\omega) = K (1 + j \omega / \omega_z) / [(1 + j \omega / \omega_{p1}) (1 + j \omega / \omega_{p2})]$ and ω_1 can be found from $H(j\omega)$

(b).(5points) Find $H(s)$ by replacing $j\omega$ by s and simplifying the terms such that $H(s) = M (N(s)/D(s))$, $N(s)$ and $D(s)$ are polynomial functions of s .

(c) (5 points) **Find output $y(t)$** for $x(t) = 10\cos(100\sqrt{10}t + \theta_1) + 5\cos(10000t + \theta_2)$.

Hint: $y(t) = A_1 \cos(100\sqrt{10}t + \theta_{y1}) + A_2 \cos(10000t + \theta_{y2})$

Find A_1, A_2 from the gain information in the Bode plot. For simplicity neglect $\theta_{y1,2}$.

Also, use an approximation as $|1 + jK| = K$ for $K > 3$.

[6] (5 points) Describe **most significant concepts** you have learned from EE103 in the Fall 2017 quarter.

